

The voters vote for A and B with a probability p and $(1-p)$ respectively equal to 0.6 and 0.4 – Now using the pool of 600 voters, we want to check out this – It’s very much like the ski wax testing example we had in class. The problem there was to see if the probability between the two skis were equal (both 0.5)- Now we want to test if the results from the pool is compatible with the probability given above.

How many voters on 600 would vote for A if the starting hypothesis was correct, ie if indeed 60% favored him?

We would expect $600 \times 0.60 = 360$ people to say “yes, I vote for A”– Now only 330 people are saying it so A is missing 30 people. Is that significant??

Well, just like for the ski wax problem, the number of choosing w votes in A in a total of N voters is $\frac{N!}{w!(N-w)!} p^w (1-p)^{N-w}$ with $p=0.6$

We saw that then the mean of the distribution was $\bar{w} = Np = 360$ and the $\sigma_w = \sqrt{Np(1-p)} = \sqrt{144} = 12$.

So missing 30 people is 2.46 sigma (standard deviations) from what was expected. Now because N is so large, the binomial distribution can be approximate by a gaussian and you can use the pages distributed in class to check what is the probability of being 2.46 sigma **below** from the expected value for a normal(gaussian) distribution. Because we are not checking the probability to be 2.46 sigma away but only that of being 2.46 sigma **below** the mean, you have to use either Appendix A divided by 2 or appendix B. This gives you a probability about 0.7%. So the result is highly significant and we can reject the claim of candidate A at better than the 1% Confidence Level.

$$2) \chi^2 = \sum_{k=1}^N \frac{(O_k - E_k)^2}{E_k} = \chi^2 / d = 10.0625 / 5 = 2.0125$$

The measured distribution can be rejected at the CL% Confidence Level, if $P(\tilde{\chi}^2 \geq \chi^2_{\alpha}) \leq CL\%$

$$P(\tilde{\chi}^2 \geq 2.0125) = 7.5\% \geq 5\%$$

The distribution cannot be rejected at the 5% level (but can be rejected at the 10% level).